

Inference at * 1
of proof for Lemma fun_exp_add-sq:

1. $n : \mathbb{Z}$
2. $0 < n$
3. $\forall m:\mathbb{N}, f, x:\text{Top}.$
 $(\text{primrec}((n - 1)+m;\lambda x.x;\lambda i.g. f \circ g)(x))$
 \sim
 $(\text{primrec}(n - 1;\lambda x.x;\lambda i.g. f \circ g)(\text{primrec}(m;\lambda x.x;\lambda i.g. f \circ g)(x)))$
4. $m : \mathbb{N}$
5. $f : \text{Top}$
6. $x : \text{Top}$

$\vdash(\text{primrec}(n+m;\lambda x.x;\lambda i.g. f \circ g)(x))$
 \sim
 $(\text{primrec}(n;\lambda x.x;\lambda i.g. f \circ g)(\text{primrec}(m;\lambda x.x;\lambda i.g. f \circ g)(x)))$
by (((RW (AddrC [2;1] (RecUnfoldC 'primrec') 0)
CollapseTHEN ((((((if (0
) =0 then SplitOnConclITE else SplitOnHypITE (0))·)
CollapseTHEN (Auto·))·)
CollapseTHEN ((Try ((Complete (Auto'))·))·))·))·)
CollapseTHEN (((
RW (AddrC [1] (RecUnfoldC 'primrec') 0)
CollapseTHEN ((((((if (0
) =0 then SplitOnConclITE else SplitOnHypITE (0))·)
CollapseTHEN (Auto·))·)
CollapseTHEN (((Try ((Complete (Auto'))·))·)
CollapseTHEN (((Reduce 0)
CollapseTHEN ((EqCD)
CollapseTHEN ((Try (Trivial))·))·))·))·))·))·)

1:

7. $\neg(n = 0)$
8. $\neg(n+m = 0)$

 $\vdash(\text{primrec}((n+m) - 1;\lambda x.x;\lambda i.g. f \circ g)(x))$
 \sim
 $(\text{primrec}(n - 1;\lambda x.x;\lambda i.g. f \circ g)(\text{primrec}(m;\lambda x.x;\lambda i.g. f \circ g)(x)))$
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